

Real Supports



نسألکم الدعاء

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إذا حملت تطبيق **RC Structures**  على تليفونك المحمول او اللوح السطحي ستستطيع أن تشغل أفلام شرح للمقاطع التي تحتوى على رمز 

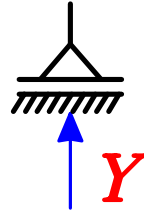
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Real Supports



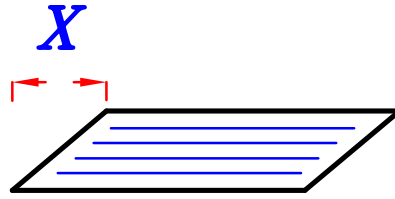
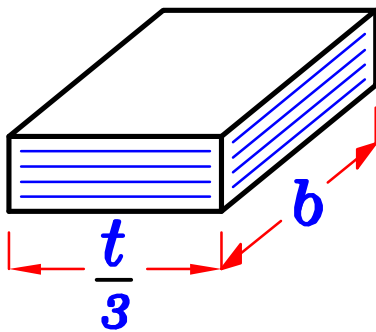
① Real Roller.



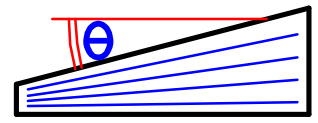
Using: *Lead Plat. or Neoprene Plate.*

Neoprene Plate.

ال **Neoprene Plate** هي ألواح من الصلب بينها شرائح من المطاط المضغوط.
توضع بين العمود و الكمره أو بين العمود و القاعده لعمل **Real Hinge**
و فائدتها أنها تسمح بالحركة الأفقيه و الدوران .

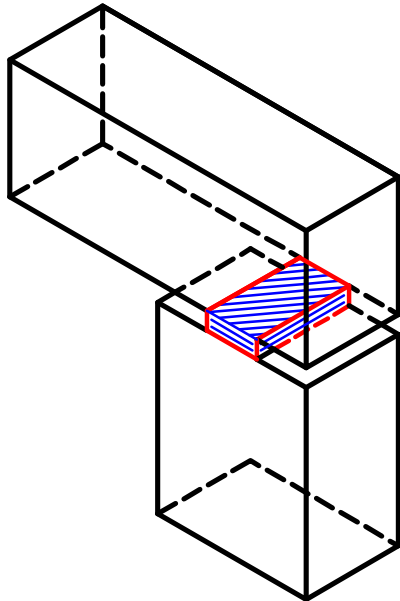


الحركة الأفقيه X

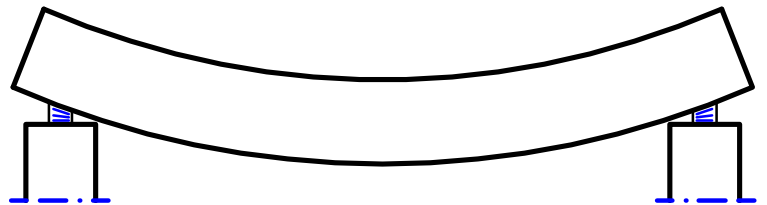


الدوران θ

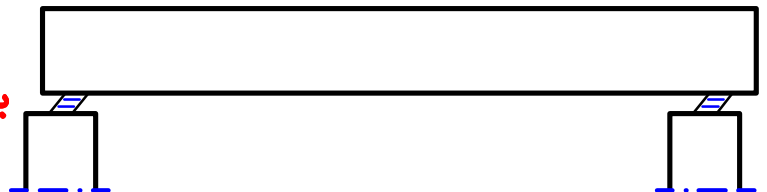
تسمح بالحركة الأفقيه و تسمح بالدوران



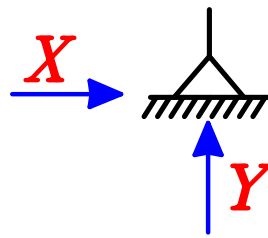
تسمح بالدوران
أي لا تنقل عزوم
على العمود



تسمح
بالحركة الأفقيه



② Real Hinge.



Types of Real hinges.

- ① *Lead Plate Hinge.*
- ② *Cross bars Hinge.*
- ③ *Spiral Hinge.*

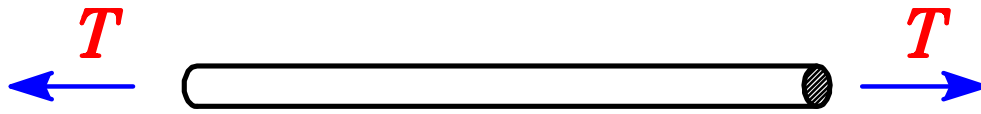
For All Types of Real Supports We have to :

- Check Bearing Stresses.*
- Calculate Stirrups.*

Allowable stress For Steel Bars.

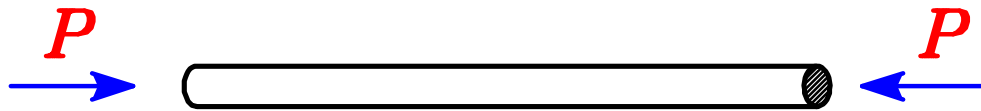
الاجهادات التي يتحملها سيخ الحديد بدون خرسانة

① *Allowable stress For Steel Bars in Tension* = $\left(\frac{F_y}{\delta_s}\right)$



$$A_s = \frac{\text{Force}}{\text{Stress}} = \frac{T}{(F_y \backslash \delta_s)}$$

② *Allowable stress For Steel Bars in Compression* = $0.60 \left(\frac{F_y}{\delta_s}\right)$

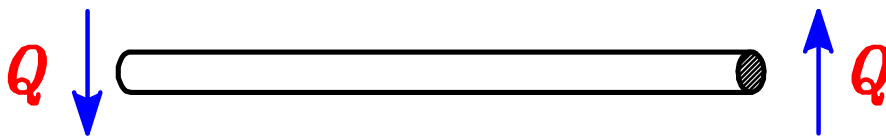


$$A_s = \frac{\text{Force}}{\text{Stress}} = \frac{P}{0.60 (F_y \backslash \delta_s)}$$

ملحوظة

إذا لم نستطع تحديد نوع القوى إذا كانت *Tension or Compression* نعتبرها *Compression*

③ *Allowable stress For Steel Bars in Shear* = $0.60 \left(\frac{F_y}{\delta_s}\right)$

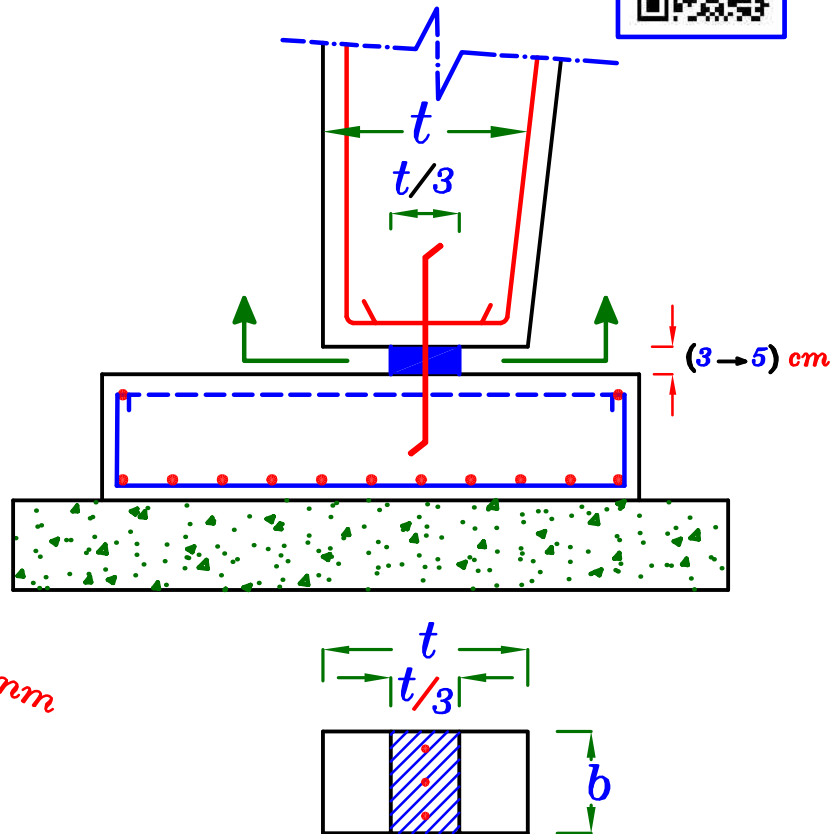
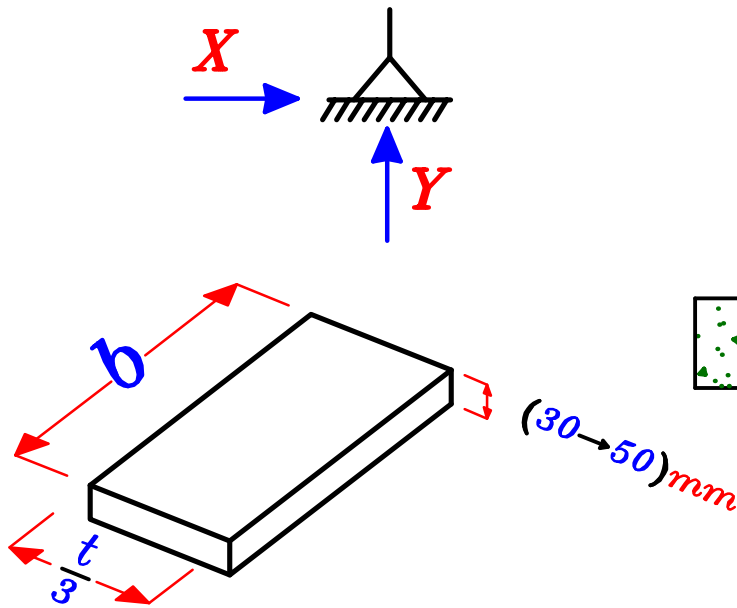


$$A_s = \frac{\text{Force}}{\text{Stress}} = \frac{Q}{0.60 (F_y \backslash \delta_s)}$$

① Lead Plate Hinge.



Using: **Lead Plat.**
OR Neoprene Plat.



- نستخدم لوح الرصاص فى نقل القوى الرأسية $Y_{U.L.}$ من العمود إلى القاعده .
و تكون أبعاد لوح الرصاص $(b * \frac{t}{3} * (30 \rightarrow 50) \text{ mm})$
- نستخدم أسياخ الحديد الرأسية **Longitudinal Bars** لنقل القوى الأفقية $X_{U.L.}$ من العمود إلى القاعده .
و لحساب مساحة أسياخ الحديد الرأسية **Longitudinal Bars**

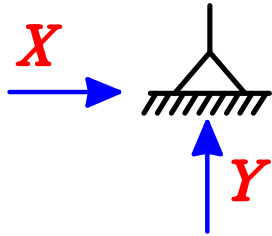
$$A_s = \frac{X_{U.L.}}{0.60 (F_y \setminus \delta_s)}$$

$$\phi > 18 \text{ mm}$$

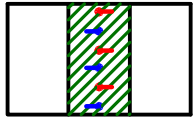
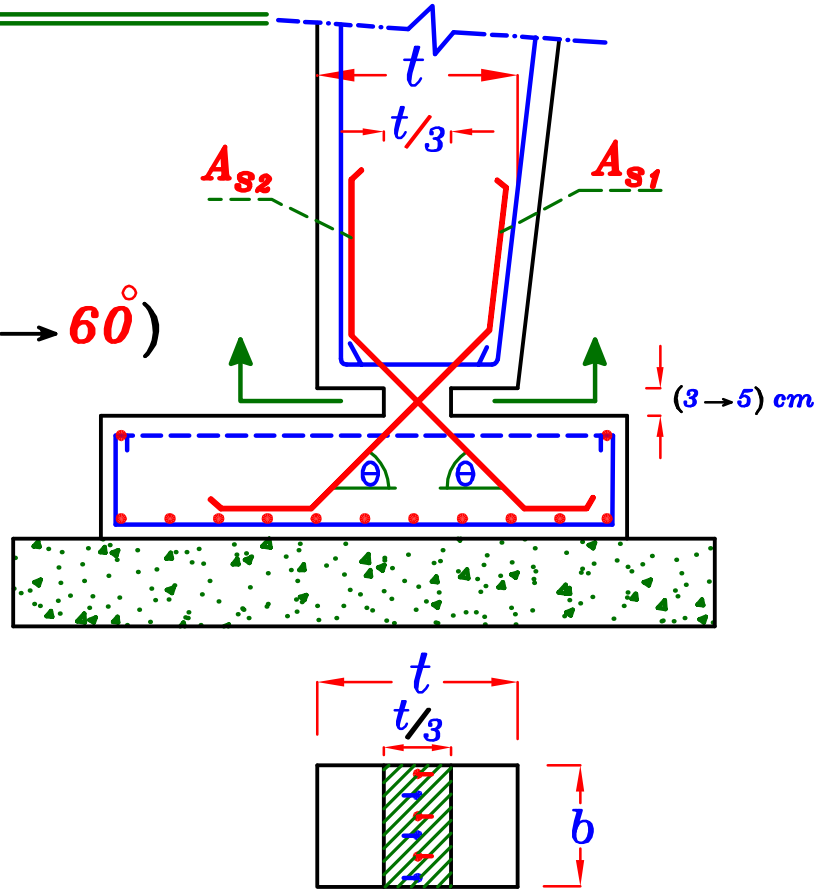
$$\text{min. } 2 \phi 20$$

Where: $0.60 (F_y \setminus \delta_s) = \text{Allowable Shear stress For Steel in U.L.D.M.}$

② Cross Bars Hinge.

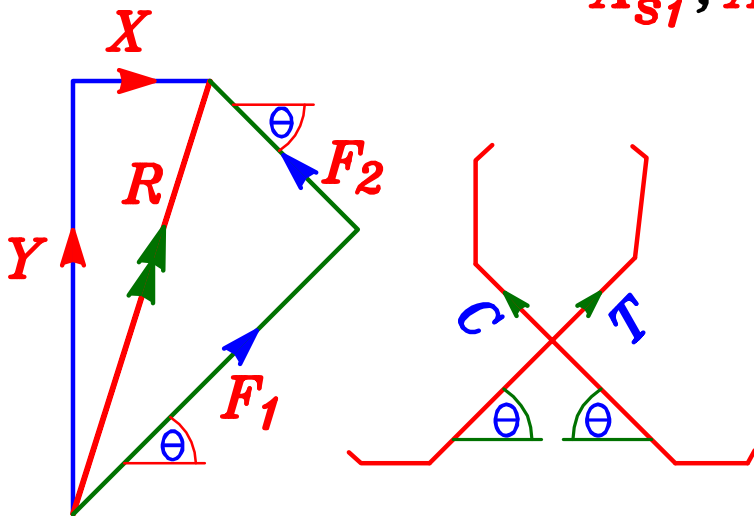


$$\Theta = (30^\circ \rightarrow 60^\circ)$$



نعتد على نقل القوى الأفقية و الرأسية بواسطة الحديد فقط .
أكبر عدد أسياخ ممكن وضعة فى ال **X-Hinge** هو ٦ أسياخ فقط
(ثلاثة جهة اليمين و ثلاثة جهة اليسار) .

لذا لا نستخدم ال **X-Hinge** إلا عندما تكون **R** صغيره .
و لحساب مساحة أسياخ الحديد A_{s1} , A_{s2}



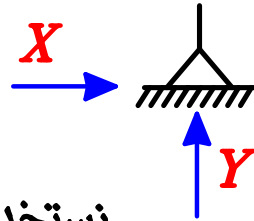
$$A_{s1} = \frac{F_{1 U.L.}}{0.6 (F_y \setminus \delta_s)}$$

$$A_{s2} = \frac{F_{2 U.L.}}{0.6 (F_y \setminus \delta_s)}$$

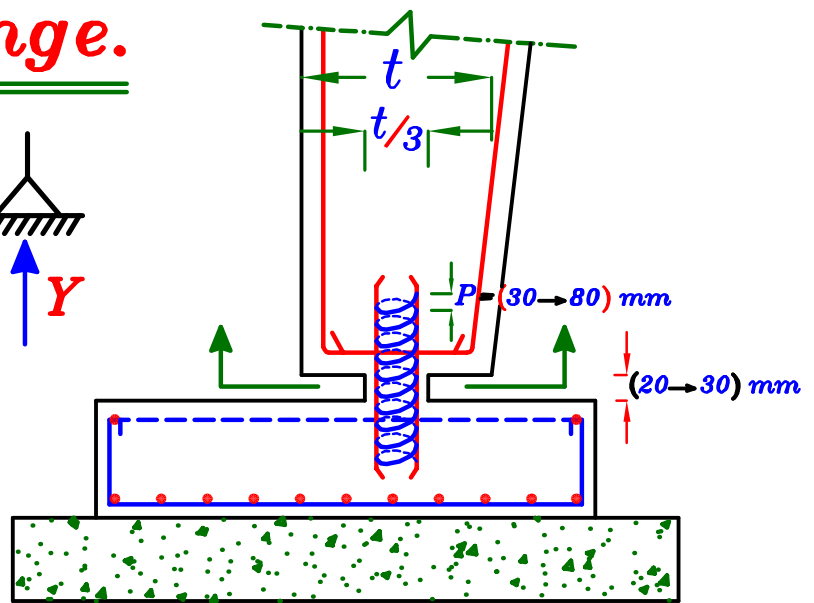
نقل من قوه تحمل أسياخ الحديد الى $0.6 (F_y \setminus \delta_s)$
لأن بعض هذه الاسياخ يتعرض لـ **Compression** .

③ Spiral Hinge.

$$Y_{U.L.} \triangleright 1800 \text{ kN}$$



نستخدم ال **Spiral Steel** لنقل القوى الرأسية فقط
و نستخدم أي **System** آخر لنقل القوى الأفقية

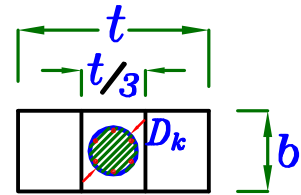


$$- D_k = \text{Diameter of the Spiral}$$

$$= b - 50 \text{ mm}$$

$$= \frac{t}{3} - 50 \text{ mm}$$

الأقل



min. no. of bars = 6 Bars

$$- A_k = \frac{\pi D_k^2}{4}$$

مساحة قلب القطاع الخرساني المحدد بدائره الكانة الحلزونية

To Get A_s $Y_{U.L.} = P_{U.L.} (\text{Spiral})$

use $P_{U.L.} = 0.35 A_k F_{cu} + 0.67 A_s F_y + 1.38 V_{sp} F_{yp}$

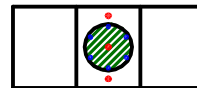
or use $P_{U.L.} (\text{Spiral}) = 1.14 (0.35 A_c F_{cu} + 0.67 A_s F_y)$

where: $A_c = A_k$, $F_y = 2400 \text{ kg/cm}^2$

To Resist $X_{U.L.}$ Use **Longitudinal bars** or **X-bars**

- IF $X_{U.L.}$ is small use **Longitudinal bars**

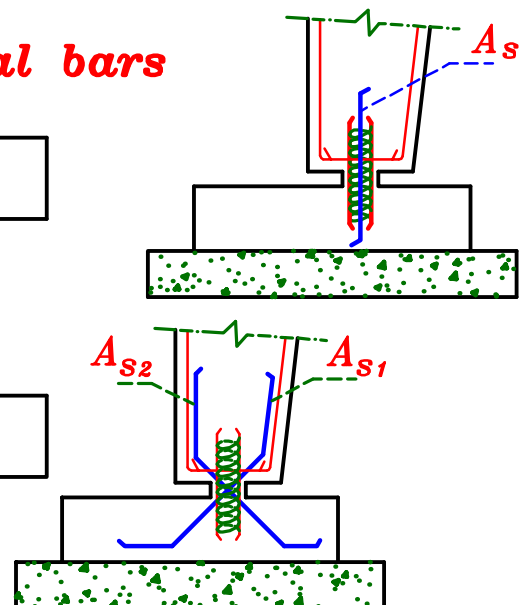
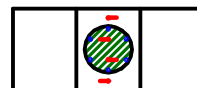
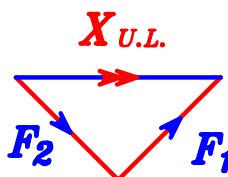
$$A_s = \frac{X_{U.L.}}{0.60 (F_y \delta_s)}$$



- IF $X_{U.L.}$ is big use **X-bars**

$$A_{s1} = \frac{F_1 U.L.}{0.6 (F_y \delta_s)}$$

$$A_{s2} = \frac{F_2 U.L.}{0.6 (F_y \delta_s)}$$

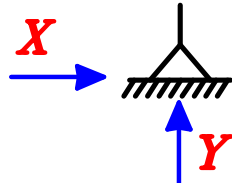


Check Bearing Stresses.

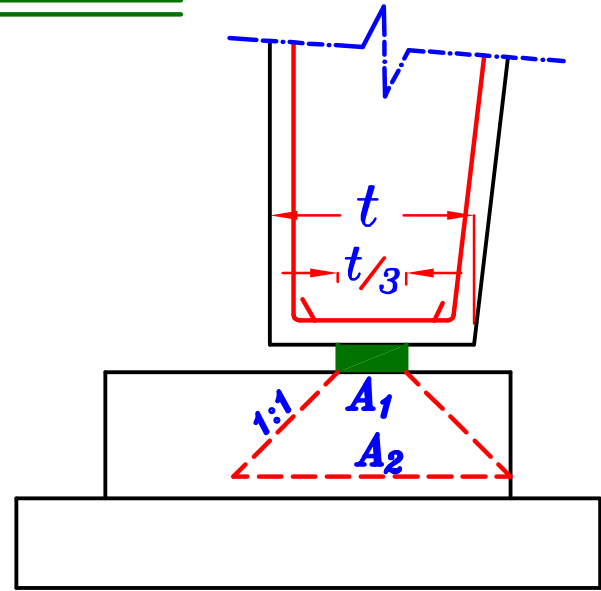
For All Types
of Real Supports.



Real Roller



Real Hinge



يجب التأكد من أبعاد ال **Real Support** $(b * \frac{t}{3})$ عن طريق **Check Bearing.**

① Calculate Allowable Bearing Stress.

$$F_{b_{all.}} = \frac{2}{3} \frac{F_{cu}}{\delta_c} \sqrt{\frac{A_2}{A_1}}$$

Where:

A_1 = مساحة التحميل Take $A_1 = (b * \frac{t}{3})$

A_2 = أكبر مساحة تحميل متماثلة مع (A_1) Take $A_2 = (b * t)$

$$\sqrt{\frac{A_2}{A_1}} > 2 \quad \text{IF we take } A_1 = (b * \frac{t}{3}), A_2 = (b * t) \rightarrow \sqrt{\frac{A_2}{A_1}} = \sqrt{3}$$

∴ Allowable Bearing Stress.

$$F_{b_{all.}} = \frac{2}{3} \frac{F_{cu}}{\delta_c} \sqrt{3}$$

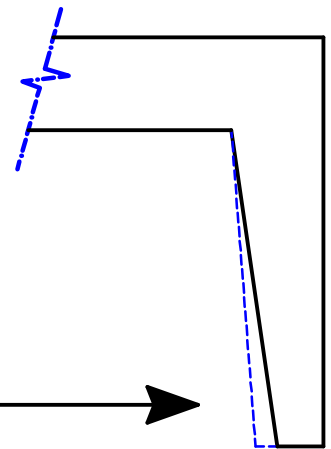
② Calculate Actual Bearing Stress.

$$F_{b \text{ act.}} = \frac{Y_{U.L.}}{(b * \frac{t}{3})}$$

To Check Bearing.

- IF $F_{b \text{ all}} \geq F_{b \text{ act}} \therefore \text{Safe}$
- IF $F_{b \text{ all}} < F_{b \text{ act}} \therefore \text{UnSafe}$

We have to Increase A_1 →



Design of stirrups.



نتيجة نقل الحمل من عرض $\frac{t}{3}$ الى عرض t
تنتج قوى شد أفقية (**Splitting Force**)

بصلة الاجهادات

Calculation the value of Splitting Force.

$$M_{a(Ext.)} = M_{a(Int.)}$$

$$M_{a(Ext.)} = \frac{Y}{2} \left(\frac{t}{4} - \frac{t}{12} \right) = \frac{Yt}{12}$$

$$M_{a(Int.)} = T \left(\frac{t}{2} \right)$$

$$\therefore M_{a(Ext.)} = M_{a(Int.)}$$

$$\therefore \frac{Yt}{12} = T \left(\frac{t}{2} \right) \longrightarrow \boxed{T = \frac{Y}{6}}$$

To Resist Splitting Force We use stirrups

$$\boxed{T = 2n A_s \left(\frac{F_y}{\delta_s} \right)}$$

Where:

n = عدد الكانات في الارتفاع t

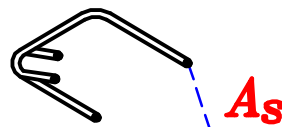
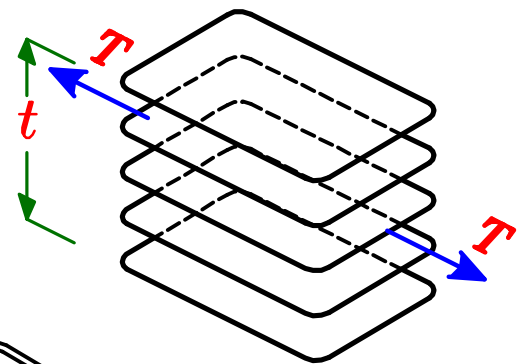
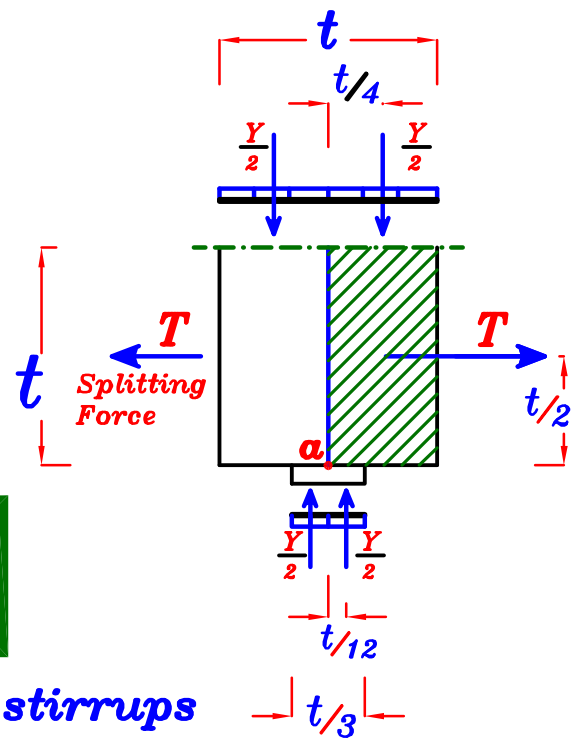
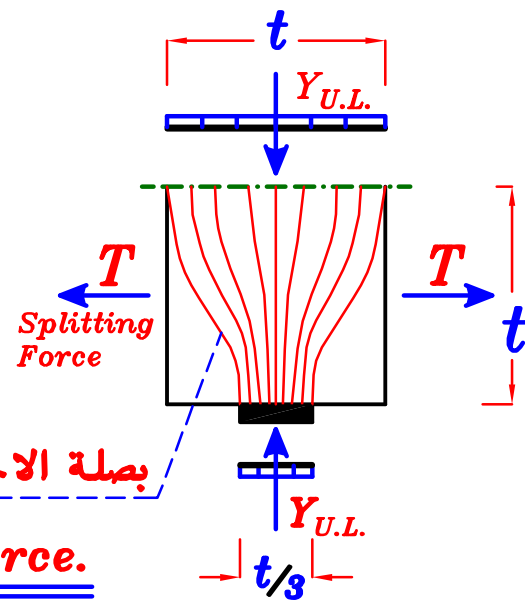
A_s مساحة سطح السيخ الواحد من الكانة

IF using $\phi 8 \longrightarrow A_s = 50.3 \text{ mm}^2$

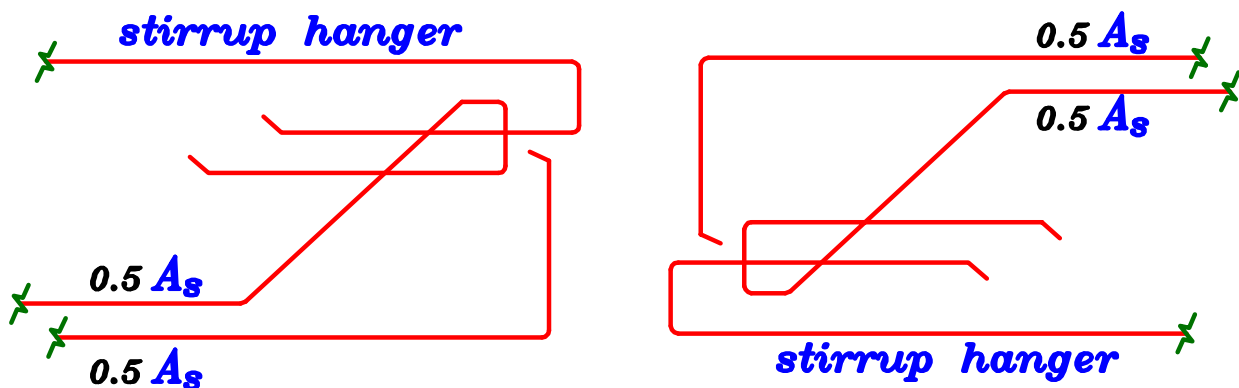
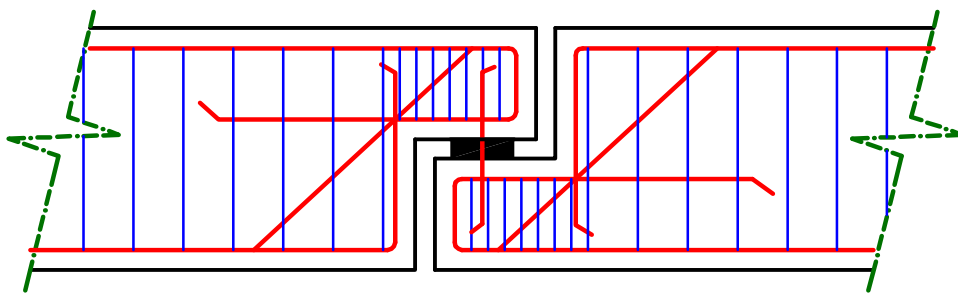
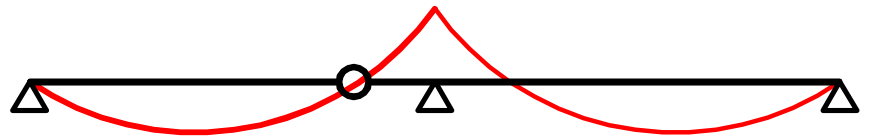
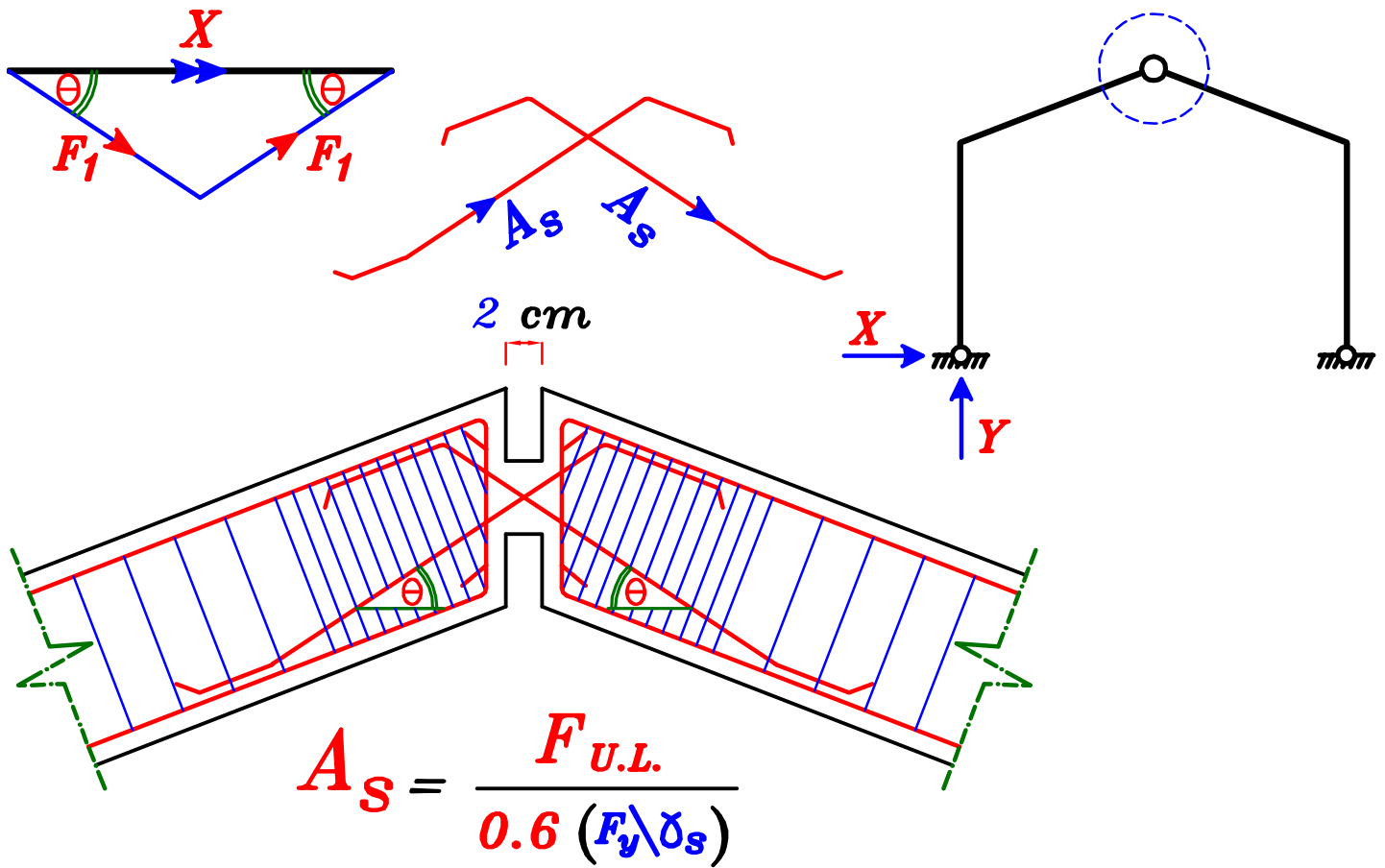
IF using $\phi 10 \longrightarrow A_s = 78.5 \text{ mm}^2$

Take $A_s = \phi 8$ OR $\phi 10 \xrightarrow{\text{Get}} n = \sqrt{\text{stirrup} \setminus t}$

\therefore Get **No. of stirrups** \ $m = \frac{1.0m}{t} * n$



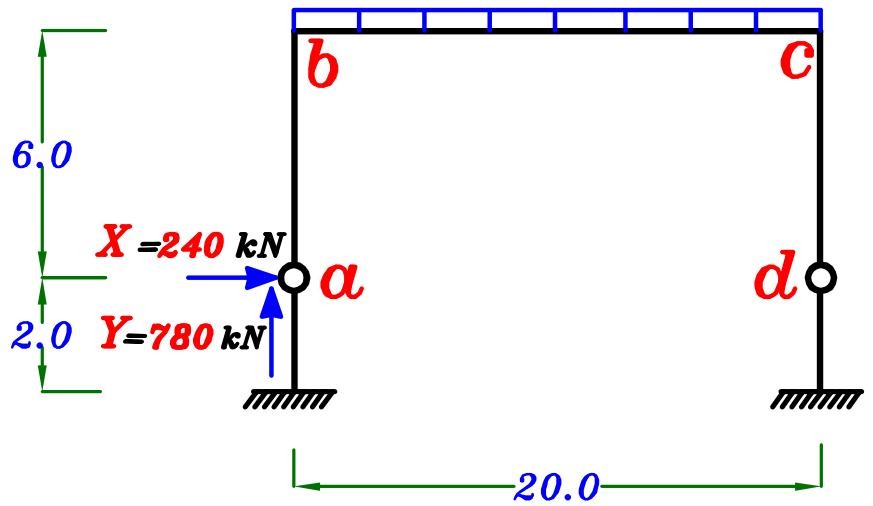
Intermediate Hinges.



Example.

* $F_{cu} = 25 \text{ N/mm}^2$

* $F_y = 360 \text{ N/mm}^2$



The shown Fixed Frame has a hinges at a & d

The reactions at the hinges From vertical load only are :

$Y = 780 \text{ kN}$, $X = 240 \text{ kN}$

- ### 1-Design the hinge at ((a))

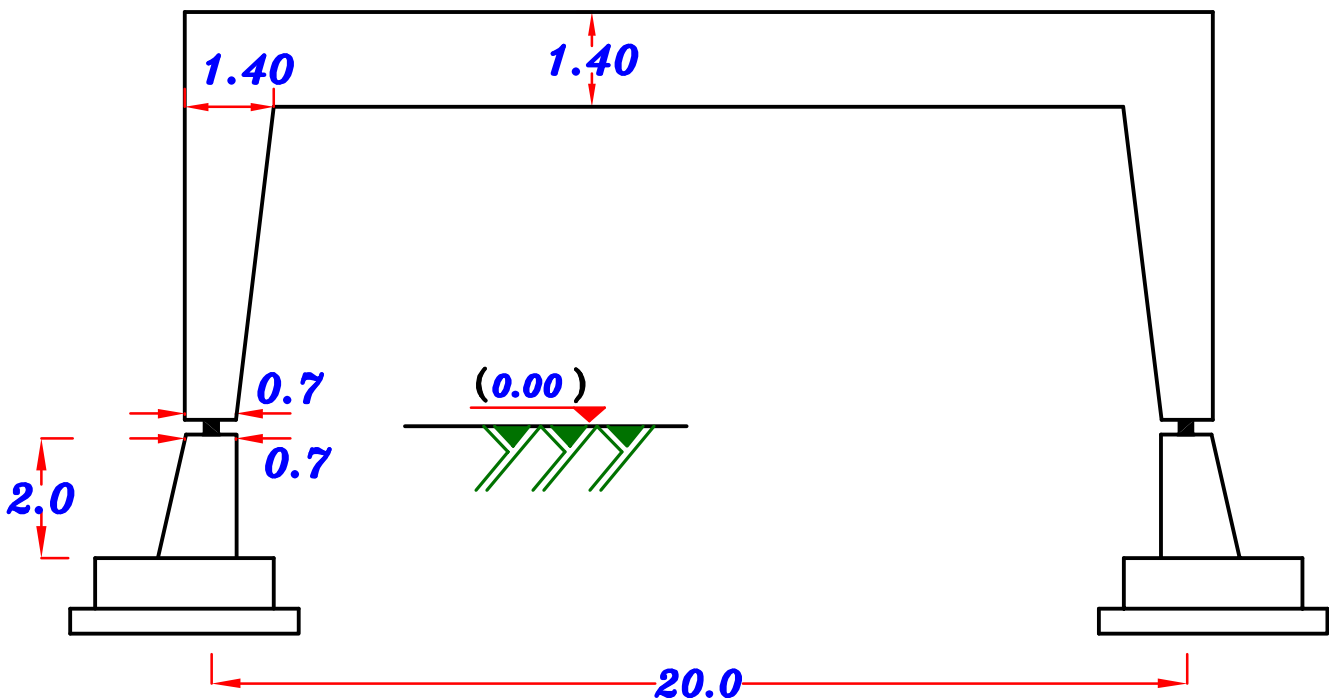
- 2-Design the column head underneath the hinge.**

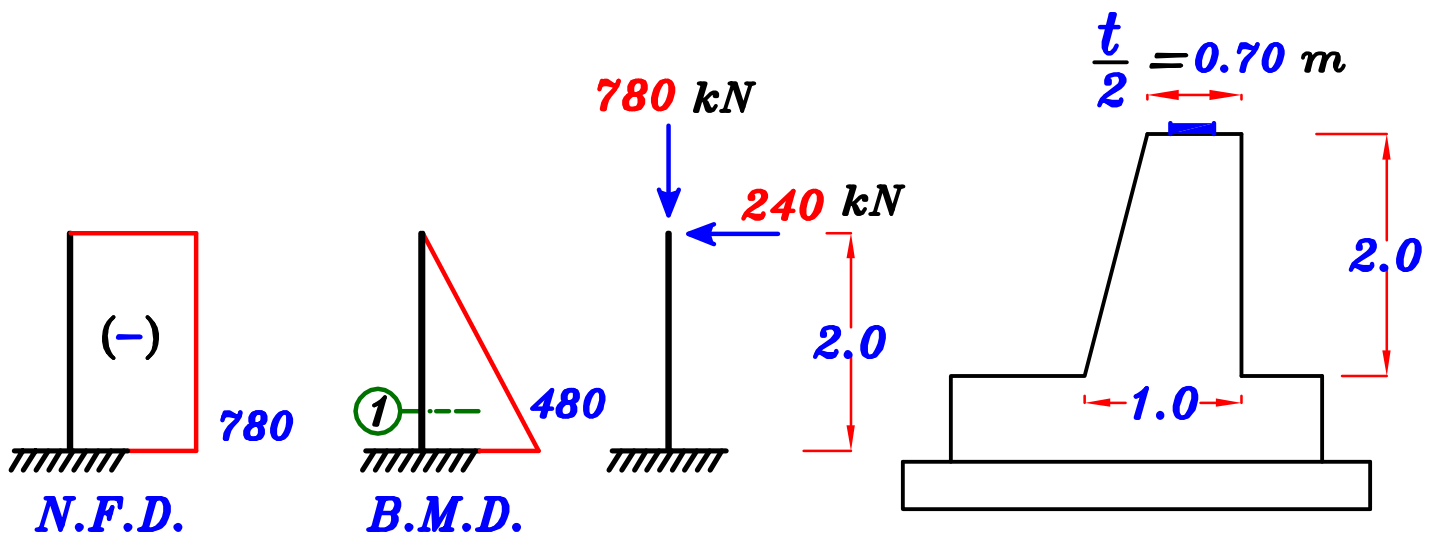
The clear height of the column head H_o is 2.0 m

- 3- Draw to scale 1:25 a sectional elevation and cross sections to show the concrete dimensions and RFT. of the hinge and the column.**

Solution.

$$\text{Take } t_{(Frame)} = \frac{L}{12 \rightarrow 14} = \frac{20}{12 \rightarrow 14} = (1.66 \rightarrow 1.42) = 1.40 \text{ m}$$





Sec. ① R-Sec. $b = 400 \text{ mm}$, $t = 1000 \text{ mm}$

$M = 480 \text{ kN.m}$, $P = 780 \text{ kN}$

Check $\frac{P}{F_{cu} b t} = \frac{780 \cdot 10^3}{25 \cdot 400 \cdot 1000} = 0.078 > 0.04$ (Don't neglect P)

$e = \frac{M}{P} = \frac{480}{780} = 0.615 \text{ m} \quad \therefore \frac{e}{t} = \frac{0.615}{1.0} = 0.615 > 0.5 \xrightarrow{\text{use}} e_s$

$e_s = e + \frac{t}{2} - c = 0.615 + \frac{1.0}{2} - 0.05 = 1.065 \text{ m}$

$M_s = P \cdot e_s = 780 \cdot 1.065 = 830.7 \text{ kN.m}$

$\therefore 950 = C_1 \sqrt{\frac{830.7 \cdot 10^6}{25 \cdot 400}} \rightarrow C_1 = 3.15 \rightarrow J = 0.757$

$\therefore A_s = \frac{M_s}{J F_y d} - \frac{P_{u.l.}}{(F_y \setminus \delta_s)} = \frac{830.7 \cdot 10^6}{0.768 \cdot 360 \cdot 950} - \frac{780 \cdot 10^3}{(360 \setminus 1.15)} = 671.0 \text{ mm}^2$

Check $A_{s_{min.}}$ $A_{s_{req.}} = 671.0 \text{ mm}^2$

$\mu_{min.} b d = \left(0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} \right) b d = \left(0.225 \cdot \frac{\sqrt{25}}{360} \right) 400 \cdot 950 = 1187.5 \text{ mm}^2$

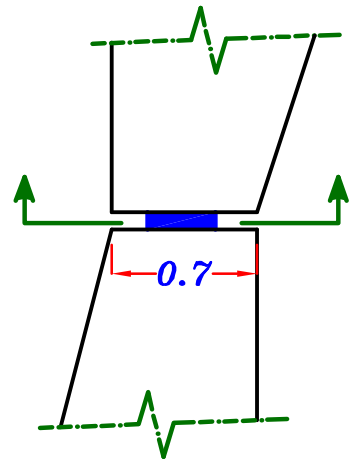
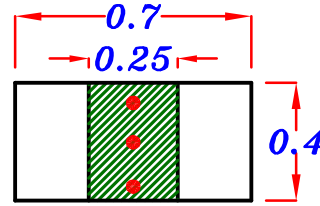
$\therefore \mu_{min.} b d > A_{s_{req.}} \xrightarrow{\text{Use}} A_{s_{min.}}$

$A_{s_{min.}} = 0.225 \cdot \frac{\sqrt{F_{cu}}}{F_y} b d = \left(0.225 \cdot \frac{\sqrt{25}}{360} \right) 400 \cdot 950 = 1187.5$ الأقل
 $1.3 A_{s_{req.}} = 1.3 \cdot 671.0 = 872.3$ } = 872.3
 st. 360/520 $\frac{0.15}{100} b d = \frac{0.15}{100} \cdot 400 \cdot 950 = 570 \text{ mm}^2$ } = 872.3 mm² الأكبر
 4 ϕ 18

Design the Hinged Support.

Using Lead Plate Hinge.

Take the dimensions of the lead Plate (**250 * 400 * 40**)



$$A_s = \frac{X_{U.L.}}{0.60 (F_y \backslash \delta_s)} = \frac{240 * 10^3}{0.60 (360 \backslash 1.15)} = 1277 \text{ mm}^2$$

3 ϕ 25

Check Bearing.

$$F_{b_{all}} = \frac{2}{3} \frac{F_{cu}}{\delta_c} \sqrt{\frac{A_2}{A_1}} = \frac{2}{3} \frac{F_{cu}}{\delta_c} \sqrt{3} = \frac{2}{3} \left(\frac{25}{1.5} \right) \sqrt{3} = 19.245 \text{ N/mm}^2$$

$$F_{b_{act.}} = \frac{Y_{U.L.}}{(b * \frac{t}{3})} = \frac{780 * 10^3}{250 * 400} = 7.80 \text{ N/mm}^2$$

$$\therefore F_{b_{all}} \geq F_{b_{act.}} \quad \therefore \text{Safe}$$

Calculation of Stirrups.

$$T = \frac{Y}{6} = \frac{780}{6} = 130 \text{ kN}$$

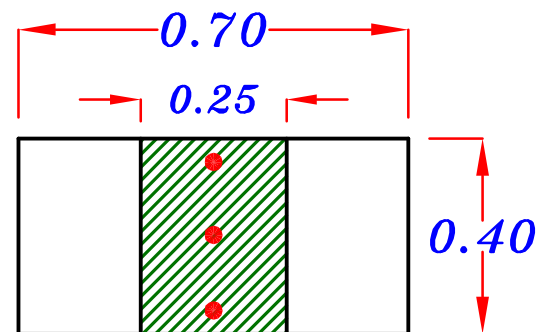
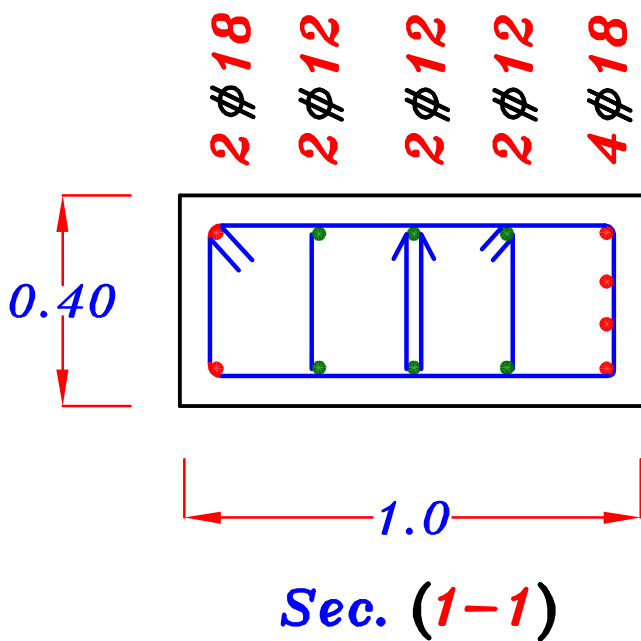
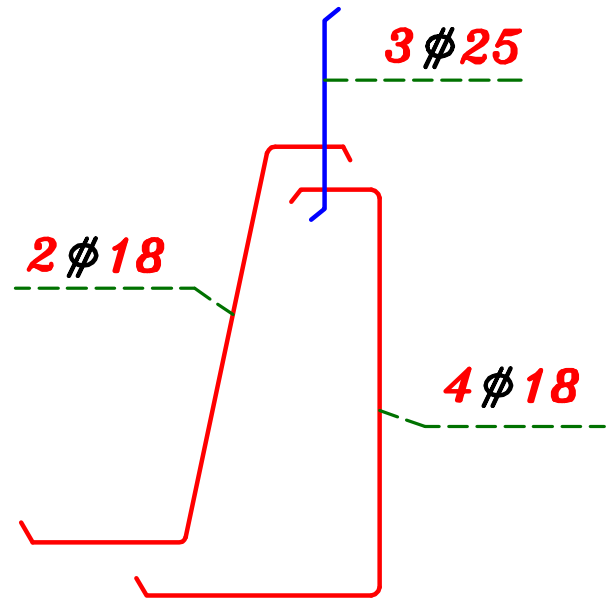
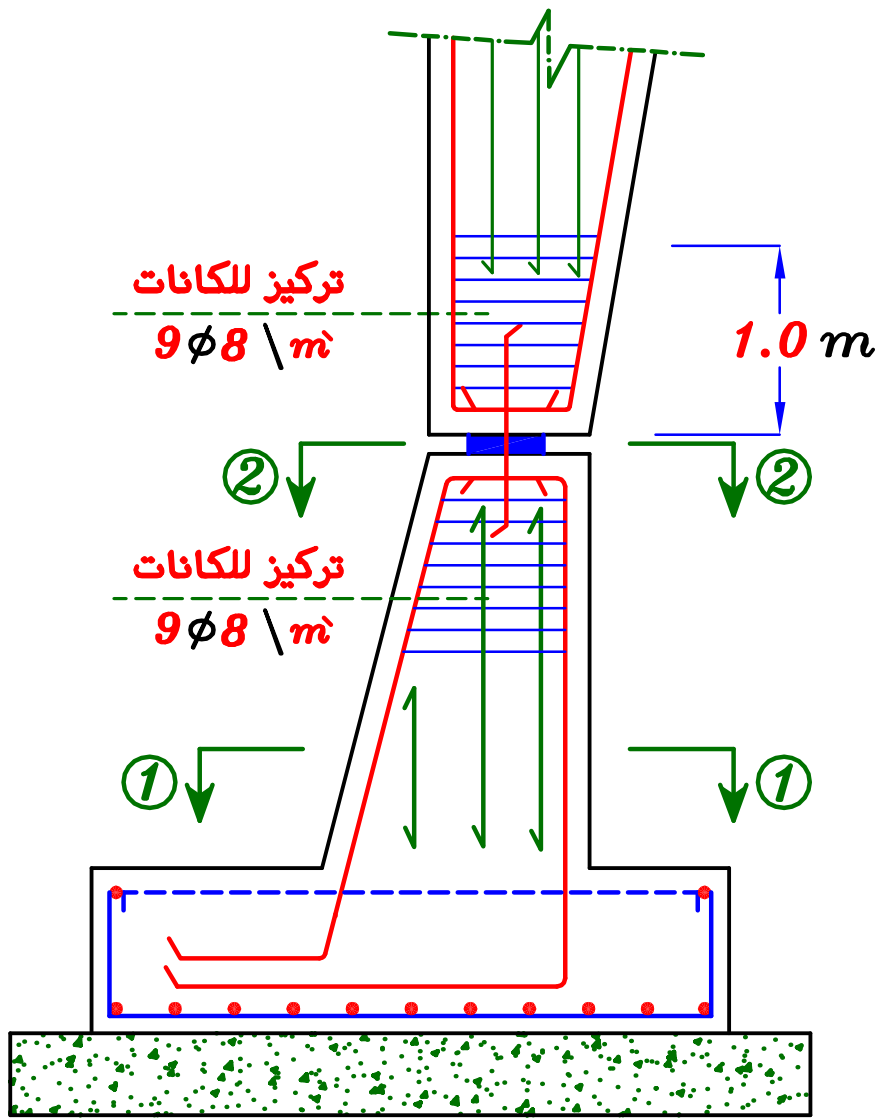
$$\therefore T = 2 n A_s \left(\frac{F_y}{\delta_s} \right) \quad \text{Take } \phi 8 \rightarrow A_s = 50.3 \text{ mm}^2$$

$$\therefore 130 * 10^3 = 2 n (50.3) \left(\frac{240}{1.15} \right) \rightarrow n = 6.19 \text{ stirrups} \backslash 0.7 \text{ m}$$

$$\therefore \text{No. of stirrups} \backslash m = \frac{1.0 \text{ m}}{0.7} * 6.19 = 8.845 \text{ stirrups} \backslash m$$

$$\therefore \text{Use Stirrups } \mathbf{9 \phi 8 \backslash m} \text{ 2 branches.}$$

RFT. of the hinge & the Column head.



Sec. (2-2)

Sec. (1-1)